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A study on the fundamental ceramic–polymer interactions in the high CeO₂-loading polyethylene glycol blend

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Abstract

Rheology of a polymer melt including ceramic particles is far cry from that of the pristine polymer phase because of the interactions between polymer and ceramic particles. This work focuses on the flow behavior of the blend comprising polyethylene glycol (PEG) melt and a fine powder (size $<5 \,\mu$ m) of cerium(IV) oxide under low shear rates. The blend containing as high as 80 wt.% (or 41.6 vol.%) of CeO₂ can still exhibit Bingham plastic response in the low shear rate range. Hence, the relative viscosities (η_{rel}) of the PEG–CeO₂ mixtures with various volume fractions of CeO₂ (ϕ) could be obtained at different temperatures, and these data were then used to simulate the rheological model developed in this work. This model was created by assuming that there are two primary forces governing the rheological behavior of the blend, which are the van der Waals attractive forces that exist among CeO₂ particles and the chemical adsorption of PEG segments on CeO₂ particles, respectively. The simulation turns out that this model matches more precisely the changes of η_{rel} versus ϕ at different temperatures than the three widely quoted models. Furthermore, the occurrence of the two stipulated forces in the PEG–CeO₂ blend has also been verified by other experimental evidences, e.g. scanning electron microscopy (SEM), X-ray diffraction (XRD), FTIR, and differential scanning calorimetry (DSC).

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1. Introduction

Porous ceramic membranes have been widely used for executing various filtration processes^{1–3} and for facilitating operations of chemical or biological reactors^{4–8} because of their remarkable chemical and thermal stability⁷ in addition to extraordinary dimensional stability. Extrusion is the most widely employed technique to the preparation of porous ceramic tubes for the use as the separation membrane or the support of chemically recognizable or reactive membranes.^{9–11} Unlike the polymer melts, the blend of a polymer melt and a ceramic powder with high volume fraction (e.g. 80–85 wt.%)

requires a much larger extrusion pressure. The polymer melt in the blend behaves very differently from itself alone in response to the applied shear stress. Nevertheless, the past experience of the polymer–ceramic interactions came primarily from the blends with low solid contents.^{12,13}

One of the most popular mathematical models describing the dependence of the shear stress on the shear rate of the blend is the Herschel–Bulkley (HB) model:^{14,15}

$$\tau = \tau_0 + K \dot{\gamma}^m \tag{1}$$

in which τ is the applied stress, τ_0 the yield stress accounting for the interactions of polymer and polymer, polymer and particle, and particle and particle under very low shear rate $\dot{\gamma}$; *K* is the consistency modulus, and the index *m* stands for the effect of high share rates. For Bingham plastic flow, *m* equals

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to unity.¹⁶ Similarly, several other mathematical models have been developed to describe the relationship between the relative viscosity (η_{rel}) of the blend and the solid powder content expressed by volume fraction (ϕ). The most feted one should be regarded as the theoretical Einstein model:¹⁶

$$\eta_{\rm rel} = 1 + 2.5\phi \tag{2a}$$

Einstein relationship is valid only for very low solid loading systems ($\phi \ll 1$) and requires the solid particles to be spherical with an identical radius.

Several empirical or semi-empirical formula have been developed thus far to describe the relationship $\eta_{rel} \sim \phi$, such as power series (Eq. (2b)), Eilers' equation (Eq. (2c)), Mooney model (Eq. (2d))¹⁷ and Krieger–Dougherty model^{15,16,18,19} (Eq. (2e)). These models can be viewed as the modified forms of the Einstein's equation by adjusting the contribution of ϕ to η_{rel} . In spite of this, these models do not justify the variations of the influence of ϕ on the defining physical chemistry basis:

$$\eta_{\rm rel} = 1 + 2.5\phi + \sum_{n=2} A_n \phi^n$$
 (2b)

$$\eta_{\rm rel} = \left(1 + \frac{2.5\phi}{1 - (\phi/\phi_{\rm max})}\right)^2 \tag{2c}$$

$$\eta_{\rm rel} = \exp\left(\frac{2.5\phi}{1 - (\phi/\phi_{\rm max})}\right) \tag{2d}$$

$$\eta_{\rm rel} = \left(1 - \frac{\phi}{\phi_{\rm max}}\right)^{K\phi_{\rm max}} \approx \left(1 - \frac{\phi}{\phi_{\rm max}}\right)^{-2.5\phi_{\rm max}}$$
(2e)

To endow the hard spheres certain sorts of surface characteristics (such as the adsorbed species), the effective solid loading (ϕ_{eff}) has been used in place of ϕ in the above equations (Eq. (3)):

$$\phi_{\rm eff} = \phi \left(1 + \frac{\delta}{R} \right) \tag{3}$$

where δ is the thickness of the average adsorbate layer and *R* is the radius of the spherical adsorbent particles.

It is generally thought that interactions between polymers and ceramic particles are the root-cause of special rheological behavior that the blend possesses, and the interactions will become more significant with increasing the volume fraction of the ceramic phase in the blend. There are basically three factors governing the interactions happening at the polymer-ceramic phase boundary: firstly, the surface area of the ceramic particles available for adsorption, particularly, for the same ceramic content, the smaller the particles the higher will be the polymer-particle interface, and therefore more viscous will be the blend;^{17,20,21} secondly, affinity of functional groups on the polymer backbone with the surface of ceramic particles or vice versa; this normally entails quasi-chemical bonding (e.g. Lewis acid-base pair) that drives the adsorption of polymer chains on ceramic particles; and thirdly, the flexibility of polymer backbone as well

as the molecular weight distribution of polymer. A polymer chain with less steric hindrance to the chain motions would have higher probabilities to form multi-adsorption sites on different ceramic particles in the blend.

Besides the polymer-ceramic interactions, attractions between ceramic particles also exist in the blend, among which van der Waals (vdw) attractive forces play the main role; other types of forces, such as electrostatic attraction or repulsion may happen depending upon the surface charge levels. The entropic depletion force which is essentially the vdw force counts on the polydispersity of the ceramic particles in the blend. Understanding how theses forces act in the nanoparticle systems has become a recent research focus.²² The vdw force is an ubiquitous force, which is generally responsible for the agglomeration of the particles and the particle-polymer separation,²³ whereas the electrostatic repulsion force is widely utilized to increase the stability of the dispersion of particles in a polymer medium.^{24–27} On the other hand, through use of a pertinent polymer, particle aggregations can be prevented by virtue of the steric repulsion of the polymer chains adsorbed on ceramic particles.²⁸

In a polymer–solid particle blend wherein if nonadsorption occurs, the polymer chains are likely to be pushed away from the space between any two particles due to the inter-particle attractions mentioned earlier. This exclusion of polymer molecules from the region leads to local agglomeration of the solid particles, and will be ending up with phase separation in the blend if "dislike" between polymer and particle determines the blend.^{29–36} In reality, adsorptions of polymers on various ceramic particles happens in major polymer–particle blends as long as the polymer chains bear organic functional groups, and what matters is the adsorption strength versus temperature, which affects the rheological behaviors of a blend. In this context, studies on the rheological behaviors of the blend can retrospectively help gaining an insight into the polymer–particle interactions.

With respect to the preparation of a polymer–ceramic blend for extrusion or molding purpose, there are several approaches: (1) introduction of the desired ceramic powder into a polymer solution (followed by removing the solvent)^{37–42} or into a polymer melt;⁴³ (2) use of organometallic polymers as pre-ceramic matrix;^{44–49} and (3) perpetrating polymerization at the surface of ceramic fine particles.^{50–53} Of these methods, direct solution mixing is obviously a simple and practical way to the preparation of extrusion feedstock.

This work prepared the polymer–ceramic blend comprising cerium oxide fine powders and polyethylene glycol (PEG) melt as a model system to study the dependence of relative viscosity of the blend on volume fraction of CeO_2 by a mathematical model. The experimental data obtained from measuring viscosity at low shear rates were employed to verify the model. This mathematic model includes the two fundamental interactions which are adsorption and vdw attraction as addressed earlier. PEG has a low and sharp melting point, surfactant-like property and ease of being burned out, these are also the merits of a desired polymer binder.⁵⁴



Fig. 1. Scanning electron micrographs of $PEG-CeO_2$ blend with 50 vol.% of CeO_2 .

2. Experimental

2.1. Chemicals

Cerium(IV) oxide (CeO₂) powder was purchased from Strem Chemicals (CAS# 1306-38-3). The powder has the average particle size of about 4.8 µm (Fig. 1) and the bulk density of 7.3. Polyethylene glycol ($\overline{M} = 15,000$) (Merck–Schuchardt), PEG-400 (Nacalai Tesque Inc.) and Tween[®] 80 (Aldrich) were used as binder, plasticizer and lubricant, respectively. All the above chemicals were used as received.

2.2. Preparation of CeO₂–PEG blend

At room temperature, CeO₂ powder was dispersed in an aqueous solution of PEG-400 and Tween® 80 (polyoxyethylene-20 sorbitan monolaurate) under continuous magnetic stirring (\sim 600 rpm). After mixing for 20 min, the resulting suspension was added into an aqueous solution of PEG-15,000 (20 wt.%) at room temperature. After mixing for 4 h, the slurry was subjected to evaporation at 80 °C till when the magnetic stirring became stuck. The concentrated slurry turned was manually blended while it was cooled down to room temperature. The remaining wet PEG-CeO2 solid was dried under vacuum for at least 72 h at room temperature to obtain the desired blend for rhelogical study. Several PEG-CeO₂ compositions were formulated by varying the content of CeO₂, which are listed in Table 1. The rheological study (shear stress versus shear rate) was carried out by examining only the blends without containing the surfactant Tween[®] 80.

2.3. Rhelogical investigation

Measurements of the steady-state viscosity were performed by using a Brookfield viscometer (Brookfield DV-II).

Table 1	
Composition of the CeO ₂ —polymer composites	

Chemical	Function	Content ^a
CeO ₂	Ceramic powder	1-80 wt.% (0.18-41.6 vol.%)
PEG-400	Plasticizer	5 wt.% of CeO ₂
PEG-15,000	Binder	Variable
Tween [®] 80	Lubricant	Variable

^a The mass densities of CeO₂ (ρ = 7.3) and PEG (ρ = 1.3) were used to compute vol.% of CeO₂.

A PEG–CeO₂ solid was loaded in a tubular aluminum sample holder, which was then placed in the accessory micro-oven. The measurement was conducted at temperatures above the melting point of PEG.

2.4. Differential scanning calorimetry (DSC) studies

DSC analysis of the PEG–CeO₂ blends was performed on the METTLER TOLEDO STAR DSC-821 scanning calorimeter in the temperature range from 25 to 100 °C. The measurement procedure included heating the sample to 100 °C (at the rate of 10 °C/min), and subsequently cooling it down to 25 °C (at the rate of -10 °C/min) to ensure all the samples under investigation have the same thermal history. The DSC data (T_g and T_m) were collected from the second scanning.

2.5. Other instrumental characterizations

X-ray diffraction (XRD) analysis was employed to examine the crystallization behavior of PEG. The analysis was carried out on a SHIMADZU XRD-6000 diffraction meter using Cu K α radiation ($\lambda = 1.54056$ Å) and the scanning speed of 2.5°/min. The scanning angle was set from 10° and 60°. The adsorption of PEG on CeO₂ was identified by the infrared spectra of PEG obtained from a Bio-Rad FTIR FTS135 spectrometer. For this characterization, only PEG (15,000) was employed to form the blend with CeO₂. The morphology of the PEG–CeO₂ blend was observed on a scanning electron microscopy (SEM) instrument (JEOL JSM-5600).

3. Results and discussion

3.1. Adsorption and van der Waals attractive forces in CeO₂–PEG blend

When the content of CeO₂ powder in the blend was raised to the comparable or higher level than that of PEG phase, the PEG phase becomes a jacket of CeO₂ particles (Fig. 1). This phenomenon shows that PEG wets CeO₂ surface well and hence a thorough mixing of both achieves readily. Likewise, XRD (Fig. 2a) characterization proved that the crystallinity of PEG phase dropped drastically even at a rather low volume fraction of CeO₂, i.e. ϕ =7.1 vol.% (or 26.8 wt.%). It could be ascribed to the strong adsorption tendency of PEG



Fig. 2. XRD of the PEG–CeO₂ blends with different CeO₂ loadings. A schematic illustration to show compressive effect on PEG coils due to instant inter-particle attraction.

segments onto CeO₂ particles, namely the orderly folding of PEG chains (crystallization) became impossible in the adsorption layer.

From the SEM image (Fig. 1), the rifts between particles were smaller than the sizes of CeO₂ particles. With this aspect ratio, the vdw attractive forces between CeO₂ particles became inevitable. As far as this type of surface–surface interaction is concerned, Myers⁵⁵ used an ideal model to describe the situation: two identical spheres of radius *R* are separated in vacuum by a distance *H*, when $H/R \ll 1$, the free energy of attraction per unit area is approximated by:

$$\Delta G^{\text{att}} = -\left(\frac{A_{\text{H}}R}{12H}\right) \left[1 + \frac{3}{4}\frac{H}{R} + \text{higher terms}\right]$$
(4a)

where $A_{\rm H} = (3/4)h\nu\alpha_0^2\pi^2 N^2$ is the Hamaker constant in vacuum (α_0 is the electronic polarizability of the atoms, $h\nu$ is related to the first ionization potential of the atoms, and N is the number of atoms in unit volume of the spheres.) When the two particles (surface) are separated by a medium, $A_{\rm H}^{\rm eff}$ is used in lieu of $A_{\rm H}$ to approximate such a more complex system, where $A_{\rm H}^{\rm eff}$ takes the mathematic form including the



Fig. 3. FT-IR spectra of PEG-CeO2 blends with different CeO2 loadings.

Hamaker constants of the two phases. Despite the fact that Eq. (4a) could describe far from precisely the free energy existing between CeO₂ particles in the blend due to geometric and compositional irregularities, it still does not lose the sense of being the ground for studying real systems. The free energy of inter-particle attraction is a crucial factor affecting the rheological responses of the composition with high CeO₂ loadings (ϕ) to shear stress.

The inter-particle attraction is considered to generate compressive force on the PEG chains (Fig. 2b). FT-IR spectra of the PEG-CeO₂ mixtures furnish the evidence to this theoretical inference (Fig. 3). The useful information from the IR analysis is the vibration absorption band of the C-O-C bond at 1112 cm^{-1} ; this band became blunt when the CeO₂ loading reached 7.1 vol.% from 1.9 vol.%, and after that, the band resumed somewhat its original shape with the increasing of CeO₂ content. This phenomenon can be understood by both the effects of inter-particle attraction and adsorption of PEG on CeO₂. Under the compression of CeO₂ particles, the bond angle of C-O-C of PEG segments would engage a certain extent of deformation, which caused changes in its stretching modulus and therefore in the shape of C-O-C IR absorption band. Although the compression on PEG became more severe with increasing ϕ of CeO₂ particles, the PEG molecules adsorbed on CeO₂ particles, on the other hand, countered the deformation of bond angles due to the "fixation" effect. The number of adsorbed PEG molecules increased with increasing CeO₂ loading in the blend, and as a result, the IR band of C-O-C vibration reflected the molecular conformation of this portion of molecules, which look more like free PEG molecules.

In addition to the XRD investigation, coherent message about structural changes of the PEG phase due to adsorption on CeO₂ particles can also be acquired from the DSC analysis. The two blends composed of 41.6 vol.% CeO₂ and the PEG phase (consisting of PEG-15,000 and PEG-400) were



Fig. 4. DSC profiles of: (a) pure PEG-15,000; (b) mixture of PEG-15,000 (80 vol.%) and PEG-400 (20 vol.%); (c) mixture of PEG-15,000 (46.72 vol.%), PEG-400 (11.68 vol.%) and CeO₂ (41.6 vol.%) made by melt mixing method; (d) the same as (c) but made by solution mixing method.

employed as the typical samples to exhibit the occurrence of strong physical adsorption (Fig. 4). Compared with the single PEG phase (a mixture of PEG-15,000 and PEG-400), the PEG phase in both blends displayed higher glass transition temperatures. It was an indication that the adsorption "bonding" restricted segment motions, e.g. rotations and creeps of PEG macromolecules, as what the "fixation" refers to in the above section. Moreover, the two different preparation procedures (solution versus fusion) also gave rise to different thermal response of the PEG phase, which revealed that the solution blending procedure resulted in a more thorough mixing blend because of higher T_g , which is ascribed to the existence of a higher PEG–CeO₂ interface in the blend.

3.2. Relative viscosity of the PEG–CeO₂ blend

The shear stress (σ)-strain rate ($\dot{\gamma}$) relationship of the melts of PEG–CeO₂ blends with different ϕ of CeO₂ all displayed Bingham fluid behavior within the low shear stress range at various temperatures (Fig. 5a-c). With respect to temperature effect, the sample containing 21.1 vol.% of CeO₂ showed a steady reduction of viscosity with raising temperature (Fig. 5a). With respect to the effect of CeO₂ loading at a fixed temperature, the higher the CeO₂ content the greater the viscosity was observed as expected; for this study two temperature points (140 and 160 °C) were examined (Fig. 5b and c). It is worthy to note that the viscosity of the blend containing 41.6 vol.% of CeO₂ became somewhat smaller than that of the blend with 21.1 vol.% of CeO₂ at 160 °C. This apparent drop in shear stress caused by raising temperature from 140 to 160 °C is deemed as the squeezing effect due to presence of the vdw attractive forces among CeO₂ particles. At 160 °C, the PEO phase became easier to free from interparticle spaces in the blend with the higher CeO₂ content under the compression as quoted earlier. In other words, the



Fig. 5. (a) Dependence of shear stress (σ) on shear rate ($\dot{\gamma}$) at different temperatures using the blend containing 21.1 vol.% of CeO₂ as the model. (b) The investigation in the effect of CeO₂ loading on $\sigma \sim \dot{\gamma}$ response at 140 °C. (c) The investigation in the effect of CeO₂ loading on $\sigma \sim \dot{\gamma}$ response at 160 °C.



Fig. 6. Dependence of the activation energy of viscous flow on the volume fraction of CeO_2 .

partial phase separation caused by raising temperature lowered down the activation energy of viscous flow. The trend revealed in this study represents a common fact: the mixing extent between a ceramic powder and a polymer phase decreases with increasing the ceramic content.

The temperature dependence of apparent viscosity of the blend melt obeyed satisfactorily the Arrhenius relation (obtained based on seven or eight temperature points in the range of 100–180 °C). The activation energy barrier of viscous flow did not vary noticeably with the CeO₂ loadings below roughly 25 vol.% (Fig. 6), which meant that there was a slippery PEG layer between CeO₂ particles before this ϕ value. A sensible explanation would be the adsorption of PEG on CeO₂ particles, which induced free volumes surrounding particles through irregular screwing up of PEG chains (Fig. 7a). The further climbing up of the activation energy symbolized formation of a physical network (Fig. 7b), in which the CeO₂ particles behaved as cross-linking points to make the viscous flow take place collectively.

A mathematical model is established to express the rheological behavior of the PEG (melt)–CeO₂ blend. The volume fraction of ceramic particles (ϕ) could be expressed by a simple mathematic formula that assumes the ceramic particles be hard spheres with identical radius of *R* and stacked with simple cubic structure:

$$\phi = \frac{(4/3)\pi}{(2+L)^3} \tag{4b}$$

However, since CeO₂ particles have irregular shapes and are polydispersed, to satisfy the model, these irregular particles can be equivalent to a certain number of spheres with radius *R* on the basis of unchanged in the surface area. As noted earlier, the *H* value is the boundary distance between two adjacent balls, L=H/R is a dimensionless quantity signifying effective distance for vdw attractive forces. Eq. (4b) can thus be rewritten as:

$$L = \left(\frac{4\pi}{3\phi}\right)^{1/3} - 2 \tag{4c}$$



Fig. 7. (a) A schematic illustration of the generation of free volume at the interfacial boundary between PEG and CeO_2 particles. (b) A schematic illustration of the formation of the physical network due to adsorption.

If ϕ is sufficiently low so as the inter-particle attraction can be neglected, the influence of the particles on rheology of the blend is thus mainly determined by the free volumes generated near the surface of individual particles as depicted in Fig. 7a. The Arrhenius equation was considered as a pertinent and succinct theoretical model⁵⁵ to describe the particle effect on viscosity. Equivalently, this concept is applied hereby to express the relative viscosity η_{rel} of the PEG–CeO₂ blend:

$$\eta_{\rm rel} = \frac{\eta}{\eta_0} = \frac{k \, \exp(E/RT)}{k_0 \, \exp(E^0/RT)} = K \, \exp\left(\frac{\Delta E}{RT}\right) \tag{5}$$

where E^0 is the energy barrier to the flow of Bingham plastic of the single PEG melt (comprising PEG-15,000 and PEG-400), *E* is the energy barrier to the Bingham flow of the PEG (melt)–CeO₂ blend, *k*, *k*₀, and *K* are constants. Therefore, ΔE reflects the contributions of polymer–particle interaction (ΔE^{ad}) and particle–particle interactions (ΔE^{vdw}) at a given temperature.

It is known that Einstein equation (Eq. (2a)) describes the hydrodynamic effect of the monodispersed hard spherical particles possessing a low volume fraction in a continuous medium. Since the CeO₂ particles used in the present real system are neither spherical ball nor monodispersed, the Einstein equation has to be modified by redefining its second terms:

$$\eta_{\rm rel}^{\rm ad} = 1 + B\phi \tag{6}$$

where *B* is the parameter including the effect of the surface area of CeO₂ particles which are the absorbent of PEG segments and therefore the cross-linking point of the physical networks formed. The physical cross-linking gives rise to a strong hydrodynamic drag on the flow of PEG melt (Fig. 7b). Moreover, *B* value also embraces the influences of irregular shape and different sizes of the CeO₂ particles on the viscosity. The superscript "ad" symbolizes the contribution of adsorption to the elastic component of the flow.

In the high-particle-loading blend, the vdw attractive forces act in the same way as the cross-adsorbed PEG chains to strengthen the network (or elastic) property of the blend, and then to impede the flow of PEG melt. From this perspective, the activation energy of viscous flow of the PEG melt (ΔE) can be correlated with the vdw attraction. Hamaker model^{26,27} describes the vdw potential (ζ) between two particles by the simple form:

$$\zeta = -\frac{A_0}{L^n} \tag{7a}$$

in which A_0 and L have been defined before, n is the parameter determined by the shape of particles:

$$\Delta E^{\rm vdw} = -k'\zeta = \frac{k'A_0}{L^n} = \frac{A}{L^n}$$
(7b)

Table 2	
Parameter values of different models under different temperature	

Model	Parameter	$140^{\circ}\mathrm{C}$	150 °C	160 °C
Eilers	$\phi_{ m m}$	0.75	0.84	0.97
Modified Eilers	$k \phi_{ m m}$	3.26 1	2.93 1	2.64 1
Mooney	$\phi_{ m m}$	0.73	0.78	0.84
Modified Mooney	$k \phi_{ m m}$	3.40 1	3.18 1	2.97 1
Krieger-Dougherty	$\phi_{ m m}$	0.48	0.50	0.53
Modified Krieger-Dougherty	$k \phi_{ m m}$	4.49 1	4.21 1	3.93 1
Our model $(n = 1)$	A B	15.93 14.90	11.69 14.51	4.88 14.49
Our model $(n=2)$	A B	111.27 12.86	85.60 13.10	39.98 13.92

The contribution of the particle–particle attraction component to retarding the viscous flow can be approximated by the linear relation between ΔE^{vdw} and ζ , k' is the proportional constant and also has the significance of the number of particle–particle pairs per unit volume. Combination of equations (4c), (5) and (7b) enables the vdw attraction to be mathematically related to the relative viscosity for the high



Fig. 8. Demonstration of the fitting results of the model developed to the experimental $\eta_{rel} \sim \phi$ data at different temperatures: (a) the model assuming spherical CeO₂ particle shape (*n*=1); (b) the model assuming rod-like CeO₂ particle shape (*n*=2); (c) dependence of the simulated parameter value *B* on temperature.

CeO₂-loading blend:

$$\eta_{\rm rel}^{\rm vdw} = \exp\left\{\frac{A}{\left[(4\pi/3\phi)^{1/3} - 2\right]^n RT}\right\}$$
(8)

Consequently, the total relative viscosity (η_{rel}) of the blend should include both η_{rel}^{vdw} (Eq. (8)) and η_{rel}^{ad} (Eq. (6)) terms, which are corresponding to ΔE^{vdw} and ΔE^{ad} , respectively:

$$\eta_{\rm rel} = \eta_{\rm rel}^{\rm ad} + \eta_{\rm rel}^{\rm vdw} \cong \exp\left\{\frac{A}{\left[(4\pi/3\phi)^{1/3} - 2\right]^n RT}\right\} + B\phi$$
(9)

Fitting the model with experimental data ($\eta_{rel} \sim \phi$ at an assigned T and n) by using the linear least square method, we were able to determine the numerical values of A and B (Table 2). The fitted value of B is much higher than the corresponding parameter in the Einstein equation (Eq. (2a)). In contrast to the original Einstein model that considers only the mechanical resistance of individual hard spheres to the flow of the continuous fluid ($\eta_{rel} = 1 + 2.5 cV_{ball}$), where c is the number of spherical balls per unit volume and V_{ball} the volume of a single sphere), the B value obtained from the simulation reflects the real resistance to the viscous flow due to the adsorption of a polymer layer on particles as well as the formation of the physical network. Values B determined at the three different temperatures (140, 150 and 160 $^{\circ}$ C) were rather similar. This outcome is indicative of a sluggish desorption of PEG from CeO2 particles with increasing temperature in the range of study. On the other hand, value A decreased sharply with increasing temperature, which suggests that the vdw attractive forces in the blend with a high ϕ are susceptible to temperature, in connection this conclusion with the preceding interpretation to the $\sigma \sim \dot{\gamma}$ response of the blend with $\phi = 41.6\%$ (in Fig. 5c), it is likely that agglomeration of CeO₂ particles due to loss of the PEO layer separating them is the reason for the reduction of A values.

Fig. 8 shows the experimental data and the simulated curves based on Eq. (9). This model fits well the experimental data. In comparison with the other three well-known models, they depart away from the experimental data more noticeably (Fig. 9). Table 2 lists numerical values of the parameters of these three models, which were obtained from simulating the experimental data. Each model had both single and double parameter forms; the latter one came from replacing the number of 2.5 with the parameter *k*, which was introduced as the crowding factor. This substitution led to the modified (or two-parameter) Eilers (Eq. (10a)),⁵⁵ Mooney (Eq. (10b))¹⁷ and Krieger–Dougherty models (Eq. (10c)),^{19,56,57} respectively:

$$\eta_{\rm rel} = \left(1 + \frac{k\phi}{1 - (\phi/\phi_{\rm max})}\right)^2 \tag{10a}$$

$$\eta_{\rm rel} = \exp\left(\frac{k\phi}{1 - (\phi/\phi_{\rm max})}\right) \tag{10b}$$



Fig. 9. (a) Comparison of the fitting results of the three common models with the experimental $\eta_{rel} \sim \phi$ data at different temperatures. (b) Dependence of simulated parameter ϕ_m value on temperature.

$$\eta_{\rm rel} = \left(1 - \frac{\phi}{\phi_{\rm max}}\right)^{-k\phi_{\rm max}} \tag{10c}$$

The modified models fit the experimental data slightly better (Fig. 10) than their corresponding unmodified models in the range of $0 < \phi_{max} \le 1$. In conclusion, the model described by Eq. (9) portrays more closely the real roles of CeO₂ particles in affecting the viscous flow of PEG melt in the blend. The roles are divided as two respects: the vdw attractive forces among CeO₂ particles and the physical network that is contingent upon the adsorption of PEO segments on CeO₂ particles.

3.3. Surfactant effect

Non-ionic surfactants bearing hydrophilic polyoxyethylene oligomer blocks have often been used as the deflocculation reagent for fine ceramic oxide powders.⁵⁸ This particular functionality is attributed to the adsorption of the hydrophilic moiety on the metal-oxide particles through the Lewis acid–base interaction or hydrogen bonding. In this way, the surfactant molecules would form one or more adsorption layers on oxide particles (Fig. 11) depending upon the amount of surfactant used. Tween[®] 80 was employed in this work as the plasticizer for the PEG–CeO₂ (41.6 vol.%) blend to reduce its low temperature extrusion viscosity. The viscous flow activation energy of the blend decreased quickly



Fig. 10. (a) Comparison of the fitting results of the modified Eilers (ME) model, Mooney (MM) model and Krieger–Dougherty (MK) model with the experimental $\eta_{rel} \sim \phi$ data at different temperatures. (b) Dependence of simulated parameter *k* value on temperature.

before 2 wt.% and level off after that (Fig. 12). This phenomenon can be understood from the multi-adsorption structure laid out in Fig. 11, firstly, the hydrophobic block of Tween[®] 80 leads to a hydrophobic slippery layer, which is responsible for the decrease of melt viscosity; secondly, only the most inner slippery layers play the primary role in lubri-



Fig. 11. A schematic illustration of the multi-layer adsorption of Tween $^{\textcircled{B}}$ 80 molecules on CeO₂ particles.



Fig. 12. Lubricating effect of Tween[®] 80 on the viscous flow of PEG–CeO₂ (41.6 vol.%) blend.

cating the flow of PEG melt as these hydrophobic layers feel the greatest torque.

4. Conclusions

The PEG-CeO₂ blends prepared via mixing CeO₂ fine powder with an aqueous solution of PEG and then removing water is an appropriate system, because of the thorough mixing extent, for the study of particle effects on viscous flow of the PEG melt under low shear rates. The XRD and DSC analyses of the resultant blends differentiated by the loading of CeO₂ (ϕ in vol.%) proved occurrence of strong adsorption of PEG chains on CeO₂ particles. The adsorption led to formation of a physical cross-linking network, especially in the high CeO₂-loading blends. On the other hand, the characteristic infrared absorption band of the PEG (ν_{C-Q-C}) undergo changes in both frequency and intensity with increasing ϕ value, which was ascribed to the existence of interparticle van der Waals attractive forces among CeO2 particles. These two fundamental interactions (adsorption and vdw attraction) are considered as the prevalent forces in such a polymer-ceramic blending system. A mathematic model expressing the relative viscosity (η_{rel}) as the function of ϕ , T, and the geometry/surface states of CeO_2 particles (*n/B*) was established on the basis of the Einstein equation and the Arrhenius relationship. In this mathematic model, the activation energy of viscous flow consists of two parts, the barrier due to formation of the physical cross-linking network $(\Delta E^{\rm ad} \sim \eta_{\rm rel}^{\rm ad})$ and the barrier due to the presence of vdw at-tractive forces $(\Delta E^{\rm vdw} \sim \eta_{\rm rel}^{\rm vdw})$. In parallel, under the low shear rates, the blends display Bingham flow behavior with respect to a series of ϕ at temperatures above the melting point of PEG. This mathematic model could more precisely match the experimental $\eta_{\rm rel} \sim \phi$ data within the designated range of shear rates and temperatures by comparing with the three commonly used models. An additional study was also carried out to understand non-ionic surfactant effect on lowering down the melt viscosity of the blends. The concept of slippery hydrophobic shell is proposed to explain the fact that there is a lowest critical concentration of surfactant.

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